

$$V(x) = x(16 - 2x)(6 - 2x)$$

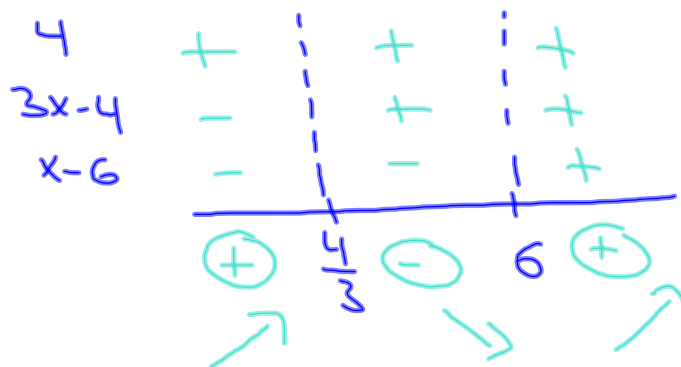
$$= x(96 - 44x + 4x^2)$$

$$V(x) = 4x^3 - 44x^2 + 96x$$

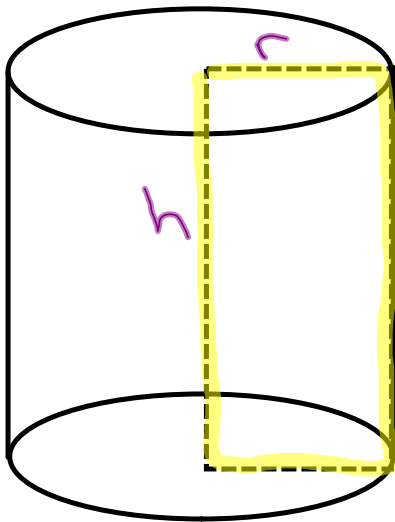
$$V'(x) = 12x^2 - 88x + 96$$

$$= 4(3x^2 - 22x + 24)$$

$$= 4(3x - 4)(x - 6)$$



max volume when $x = \frac{4}{3}$



$$V = \pi r^2 h$$

$$V = \pi r^2 (12 - r)$$

$$V = 12\pi r^2 - \pi r^3$$

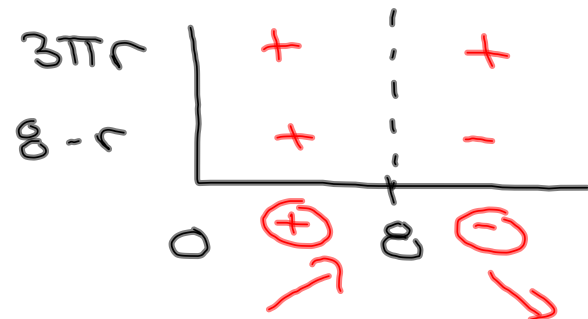
$$\frac{dV}{dr} = 24\pi r - 3\pi r^2$$

$$= 3\pi r(8 - r)$$

$$2r + 2h = 24$$

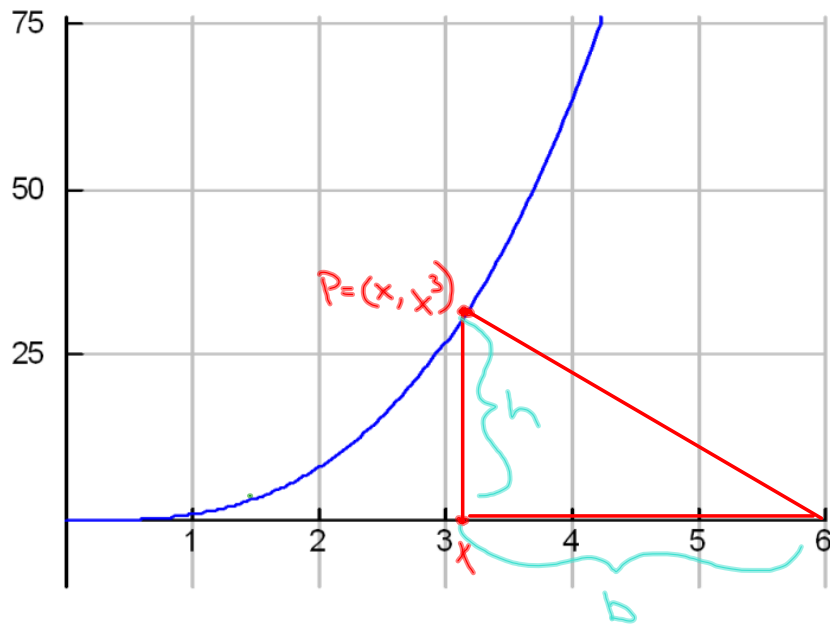
$$r + h = 12$$

$$h = 12 - r$$



max Volume when

$$r = 8, h = 4$$



$$\text{Area} = \frac{1}{2} \cdot b \cdot h$$

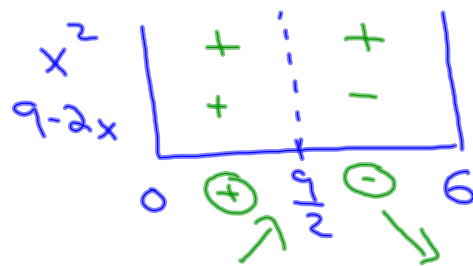
$$A = \frac{1}{2} (6-x) x^3$$

$$= \frac{1}{2} x^3 (6-x)$$

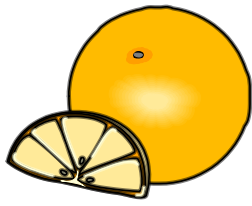
$$A = 3x^3 - \frac{1}{2} x^4$$

$$A' = 9x^2 - 2x^3$$

$$= x^2 (9 - 2x)$$



max area when $x = \frac{9}{2}$



$I = \text{yield} \cdot \text{Price}$

$$I = (80 + 10w)(40 - 2w)$$

$$I = 3200 + 240w - 20w^2$$

$$I' = 240 - 40w$$

$$= 40(6 - w)$$

